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**Sean McGuinness\***, Dept. of Mathematics, Dartmouth College, Hanover, NH 03755. *Ore-Type and Dirac-Type Theorems for Matroids.*

In this talk, we shall show that well-known theorems of Dirac and Ore concerning cycles through vertices in a graph can be extended to binary matroids having no  $F_7^*$ -minor. In one result, we show that for any collection  $\mathcal{A}^*$  of cocircuits in a connected binary matroid  $M$  having no  $F_7^*$ -minor, there is a circuit intersecting all cocircuits of  $\mathcal{A}^*$  if either one of two things hold:

- (i) For any two disjoint cocircuits  $A_1^*$  and  $A_2^*$  in  $\mathcal{A}^*$  it holds that  $r^*(A_1^*) + r^*(A_2^*) > r^*(A_1^* \cup A_2^*)$ .
- (ii) For any two disjoint cocircuits  $A_1^*$  and  $A_2^*$  in  $\mathcal{A}^*$  it holds that  $r(A_1^*) + r(A_2^*) > r(M)$ .

In a second result, we show that a theorem of Dirac for graphs can be extended to matroids by showing that for any  $k$  cocircuits of a  $k$ -connected binary matroid  $M$  having no  $F_7^*$ -minor, there is a circuit which intersects them.

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