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For a complex hyperplane arrangement in \mathbb{C}^ℓ with complement $X(A)$ and cohomology ring A , the resonance variety $R^k(A)$ is the loci of $a \in A_1$ such that the cohomology $H^k(A, \wedge a)$ of the Aomoto complex is nonvanishing. For example, $R^1(A)$ is the union of the tangent cones at $\mathbf{1}$ to the characteristic varieties of $\pi_1(X(A))$. Recent work shows that $R^1(A) = V(\text{ann}(\text{Ext}^{\ell-1}(F(A), S)))$, where S is a symmetric algebra and $F(A)$ is a finitely generated, graded S -module depending only on the cohomology ring of $X(A)$.

We generalize this result on the cohomology ring of an arrangement complement in two directions; we replace $F(A)$ with an arbitrary S -module M ; if $\text{pdim}(M) = \ell$ then

$$R^k(M) = \bigcup_{k' \leq k} V(\text{ann}(\text{Ext}^{\ell-k'}(M, S))),$$

where $R^k(M)$ is defined in terms of Koszul cohomology. The Cartan–Eilenberg spectral sequence gives

$$\text{Ext}^i(\text{Ext}^j(M, S), S) \Rightarrow M,$$

yielding relationships between the $R^k(M)$ related to the filtration of M . (Received September 15, 2006)