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Let  $A$  be an algebra over a field  $F$ . We do not assume  $A$  to be commutative. A product  $R \cdot L$  of a right ideal  $R$  of  $A$  with a left ideal  $L$  of  $A$  is the set of all sums of elements  $x \cdot y$  where  $x \in R$  and  $y \in L$ . Clearly,  $R \cdot L$  is a subset of  $A$  and also is a subset of  $R$  and of  $L$ .

Let  $M, N$  be right ideals of  $A$  and  $P, K$  be left ideals of  $A$ . It's easy to show that

$$(M \cap N) \cdot P \subset (M \cdot P) \cap (N \cdot P)$$

$$(M \cap N) \cdot P \subset (M \cdot P) \cap (M \cdot K)$$

If  $A$  is the commutative algebra of all polynomials in variables  $x, y$  over  $F$ ,  $M = x \cdot A$ ,  $N = y \cdot A$  and the ideal  $P$  is the set of all polynomials with no free term [their monomials are divisible by  $x$  or  $y$ ] then  $M \cap N = (x \cdot y) \cdot A$  and so  $(M \cap N) \cdot P$  is the set of all polynomials such that their monomials are of total degree 3 or more so it does not contain  $x \cdot y$  but  $M \cdot P$  contains  $x \cdot y$  and  $N \cdot P$  contains  $x \cdot y$  so  $(M \cdot P) \cap (N \cdot P)$  contains  $x \cdot y$ . So in this case

$$(M \cap N) \cdot P \neq (M \cdot P) \cap (N \cdot P)$$

In this work we find a very general sufficient condition on  $A$  so that

$$(M \cap N) \cdot P = (M \cdot P) \cap (N \cdot P)$$

and

$$(M \cap N) \cdot P = (M \cdot P) \cap (M \cdot K)$$

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