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Let G be a reductive algebraic group defined over an algebraically closed field k of characteristic p , which we assume is *good* for G . An involution θ of G determines the fixed point subgroup $K = G^\theta$, and a decomposition $\mathfrak{g} = \mathfrak{k} \oplus \mathfrak{s}$ of $\mathfrak{g} = \text{Lie}(G)$ into ± 1 -eigenspaces for $d\theta$. Here $\mathfrak{k} = \text{Lie}(K)$, while the -1 -eigenspace \mathfrak{s} is the “infinitesimal” symmetric space which identifies with the tangent space at the identity to the symmetric space G/K . For $\mathcal{N}(\mathfrak{g})$ the nullcone of \mathfrak{g} , take $\mathcal{N}(\mathfrak{s}) = \mathfrak{s} \cap \mathcal{N}(\mathfrak{g})$. The adjoint action of G on $\mathcal{N}(\mathfrak{g})$ yields an action of K on $\mathcal{N}(\mathfrak{s})$.

Drawing parallels with the well-known and rich study of the G -orbits on $\mathcal{N}(\mathfrak{g})$, we consider desingularizations of orbit closures $\overline{\mathcal{O}}$ for \mathcal{O} a K or K° -orbit in $\mathcal{N}(\mathfrak{s})$, and discuss applications to topics such as the normality of $\overline{\mathcal{O}}$ and cohomological interpretations of rings of functions for these orbits. (Received September 26, 2006)