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**John E. Ehrke\*** (john\_ehrke@baylor.edu), John E. Ehrke, 2414 S. University Parks Dr. #2A, Waco, TX 76706. *Positive Solutions of an  $n^{\text{th}}$  Order Boundary Value Problem: A Functional Approach.*

We apply a well-known fixed point theorem to guarantee the existence of a positive solution for the  $n^{\text{th}}$  order differential equation

$$y^{(n)} + f(y(t)) = 0, \quad t \in [0, 1],$$

having boundary conditions,

$$\begin{aligned} y^{(r_i-1)}(0) &= 0, \quad 1 \leq i \leq k, \\ y^{(s_j-1)}(1) &= 0, \quad 1 \leq j \leq n - k, \end{aligned}$$

where  $\{s_1, \dots, s_{n-k}\}$  and  $\{r_1, \dots, r_k\}$  form a partition of  $\{1, \dots, n\}$  such that  $r_1 < \dots < r_k$ ,  $s_1 < \dots < s_{n-k-1}$ , and  $\{r_{k-1} \dots r_k\} \neq \{n-1, n\}$  and  $\{s_{n-k-1}, s_{n-k}\} \neq \{n-1, n\}$ . Under these assumptions we show this boundary value problem has a positive solution for all  $n \geq 2$ . Some consideration is given to bounds for the solution. (Received September 14, 2006)