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J Marshall Ash* (mash@math.depaul.edu), DePaul University, Department of Mathematics, Chicago, IL 60614. *A halfspace is a multiplier on $L^p(\mathbb{T}^d)$.*

The Hilbert transform H is given by the multiplier operator $-i \operatorname{sgn}(n)$. The behavior of this operator is equivalent to that of the multiplier operator $P = \frac{\operatorname{Identity} + iH}{2}$ which maps a function $f \in L^p(\mathbb{T})$, $f(x) = \sum_{n=-\infty}^{\infty} \hat{f}(n) e^{2\pi i n x}$ to $Pf(x) = \sum \chi_S(n) \hat{f}(n) e^{2\pi i n x}$, where χ_S is the characteristic function of $\{n \in \mathbb{Z} : n \cdot 1 > 0\}$. A theorem of M. Riesz asserts that for $1 < p < \infty$, P is bounded on $L^p(\mathbb{T})$. A natural d dimensional analogue of P is multiplication by the characteristic function of a halfspace, i.e. the mapping of $\sum_{n \in \mathbb{Z}^d} \hat{f}(n) e^{2\pi i n \cdot x}$ to $\sum \chi_S(n) \hat{f}(n) e^{2\pi i n \cdot x}$, where χ_S is the characteristic function of $\{n \in \mathbb{Z}^d : n \cdot u > c\}$, where c is a real number and u is a unit vector in R^d . We have proved that this mapping is bounded on $L^p(\mathbb{T}^d)$. We will discuss the part of the proof which reduces the case of general c to the special case of $c = 0$. (Received September 25, 2006)