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Midway Road, Menasha, WI 54952-1297. *The submartingale problem for a class of degenerate elliptic operators.*

We consider the degenerate elliptic operator acting on C_b^2 functions on $[0, \infty)^d$:

$$\mathcal{L}f(x) = \sum_{i=1}^d a_i(x) x_i^{\alpha_i} \frac{\partial^2 f}{\partial x_i^2}(x) + \sum_{i=1}^d b_i(x) \frac{\partial f}{\partial x_i}(x),$$

where the a_i are continuous functions that are bounded above and below by positive constants, the b_i are bounded and measurable, and the $\alpha_i \in (0, 1)$. We impose Neumann boundary conditions on the boundary of $[0, \infty)^d$. There will not be uniqueness for the submartingale problem corresponding to \mathcal{L} . If we consider, however, only those solutions to the submartingale problem for which the process spends 0 time on the boundary, then existence and uniqueness for the submartingale problem for \mathcal{L} holds within this class. Our result is equivalent to establishing weak uniqueness for the system of stochastic differential equations

$$dX_t^i = \sqrt{2a_i(X_t)} (X_t^i)^{\alpha_i/2} dW_t^i + b_i(X_t) dt + dL_t^{X^i}, \quad X_t^i \geq 0,$$

where W_t^i are independent Brownian motions and $L_t^{X^i}$ is a local time at 0 for X^i . (Received September 20, 2006)