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We begin by recalling the vorticity formulation for Euler flow on a Riemannian 2-manifold  $M$  with boundary. This gives an ODE on the space of (smooth) functions on  $M$ . We define a Symplectic Approximation to this ODE to be a finite dimensional hamiltonian system together with a symplectic integration algorithm for the hamiltonian whose flow can be considered as an approximation to the original ODE. As the main example of symplectic approximation we show that given a finite piecewise linear triangulation of  $M$ , we can construct a 4-tuple  $(\mathfrak{g}, Q, H, \sigma)$ , where  $\mathfrak{g}$  is a compact Lie algebra,  $Q : \mathfrak{g}^* \rightarrow C^0(M)$  is an approximation map,  $H : \mathfrak{g}^* \rightarrow \mathbb{R}$  is a quadratic hamiltonian, and  $A$  is a symplectic integration algorithm for  $H$ . We conclude with animations demonstrating the approximation in action. (Received September 25, 2006)