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**Antonia E. Cardwell\*** ([antonia.cardwell@millersville.edu](mailto:antonia.cardwell@millersville.edu)), Department of Mathematics, Millersville University of Pennsylvania, P.O. Box 1002, Millersville, PA 17551. *Some constructive proofs of Bollobás' Extension to the Bishop-Phelps Theorem for the spaces  $C(K)$  and  $c_0$ .*

Constructive proofs of Bollobás' result for the real spaces  $C(K)$ , where  $K$  is a compact set in a Banach space, and  $c_0$  will be presented in this session. In 1961 E. Bishop and R. R. Phelps proved that every real Banach space is subreflexive; in other words, every functional can be approximated by a norm-attaining functional of the same norm. In 1970, B. Bollobás refined the result to show that if  $f$  is a norm one functional that "almost" attains its norm at a point  $x$  then  $f$  can be approximated by a norm attaining norm one functional that attains its norm at a point close to  $x$ . The original proof of the Bishop-Phelps result is an existence argument and the exact structure of the norm-attaining functional is not given. One possible structure will be examined in each of the above-mentioned spaces. (Received September 16, 2007)