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Douglas Cenzer* (cenzer@ufl.edu), Department of Mathematics, P.O. Box 118105, University of Florida, Gainesville, FL 32611-8105, and **S. Ali Dashti**. *Decidability of countable closed subshifts*. Preliminary report.

A closed subset of $2^{\mathbb{N}}$ is a *subshift* if it is closed under the shift operator σ , where $\sigma(X(0), X(1), \dots) = (X(1), X(2), \dots)$. The authors recently showed (Math. Logic Quarterly, 2008) that there exists an effectively closed (Π_1^0) subshift with no computable member. We now investigate countable Π_1^0 subshifts. It is shown, for example, that any Π_1^0 subshift of rank one is decidable, whereas there is an undecidable Π_1^0 subshift of rank two. (Received September 10, 2008)