

1046-05-1278

**James N Brantner\*** (jbrantne@erskine.edu), PO Box 1001, CPO 229, Due West, SC 29639.

*On Seymour's Second Neighborhood Conjecture.*

Let  $D$  be a simple digraph without loops or digons (i.e. if  $(u, v) \in E(D)$ , then  $(v, u) \notin E(D)$ ). For any  $v \in V(D)$  let  $N_1(v)$  be the set of all vertices at out-distance 1 from  $v$  and let  $N_2(v)$  be the set of all vertices at out-distance 2. We provide sufficient conditions under which there must exist some  $v \in V(D)$  such that  $|N_1(v)| \leq |N_2(v)|$ , as well as examine properties of a minimal graph which does not have such a vertex. We show that if one such graph exists, then there exist infinitely many strongly-connected graphs having no such vertex. (Received September 15, 2008)