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The continued fraction expansion of $\sqrt{2}$ gives a sequence of rational approximations (p_n/q_n) to $\sqrt{2}$. But we can also look at it this way: we get a sequence of integer vectors (p_n, q_n) that are exceptionally close to being perpendicular to $(1, -\sqrt{2})$. What happens if we look for integer vectors $b = (b_0, \dots, b_{n-1})$ exceptionally close to being perpendicular to $(1, \alpha, \dots, \alpha^{n-1})$, when α is an algebraic integer of degree n ?

If we call suitable lists b of integers *good*, we can then ask how we might find good b and what they are like. We can find them computationally by way of a lattice reduction trick. We can find them via number theory, because they have a special structure: the associated algebraic integer $\beta = \sum b_k \alpha^k$ has small *norm*, and apart from β itself, the algebraic conjugates of β have comparable absolute values.

We can also say where to find them: The *scaled coefficient lists* $|\beta|^{1/(n-1)}b$ associated with b sit very nearly on one of a finite number of surfaces λS in \mathbb{R}^n , where S is a hyperboloid(*) that depends on α . (Received September 16, 2008)