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**Brian C. Dietel\*** (dietelb@onid.orst.edu), Oregon State University, Department of Mathematics, 368 Kidder Hall, Corvallis, OR 97331. *Mahler's order functions and  $p$ -adic algebraic approximation.*

If  $P$  is a polynomial of degree  $d$  define  $\Lambda(P)$  to be the product of  $2^d$  with the sum of the absolute value of the coefficients of  $P$ . In a 1971 paper Kurt Mahler defined the “order function” of each complex number  $\alpha$  by  $O(u|\alpha) = \sup \log |\frac{1}{P(\alpha)}|$  where the supremum is taken over all integer polynomials  $P$  satisfying  $\Lambda(P) \leq u$  and  $P(\alpha) \neq 0$ . By placing a partial order on the order functions Mahler induced a classification of the complex numbers. We will consider the properties of order functions when  $\alpha$  is a  $p$ -adic number. Many of the results previously obtained in the real case still hold for the  $p$ -adics. However, the unique properties of the  $p$ -adic numbers result in several exceptions. (Received September 03, 2008)