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Taiji Tsutsui* (tsutsuit@my.hiram.edu), PO Box 1234, Hiram, OH 44234, and **Rachel Ellen Cranfill** (rachel_cranfill@hmc.edu). *The Minimum Semidefinite Rank of a Graph.*

A Hermitian matrix is a complex matrix that is equal to its conjugate transpose. Given an n by n Hermitian matrix A , we associate a graph $G(A)$ whose vertex set is $\{1, \dots, n\}$ and whose edge set consists of unordered pairs $\{i, j\}$ if and only if the (i, j) th entry of A is nonzero. The collection of Hermitian positive semidefinite matrices that share a common graph G is denoted $P(G)$. Define the minimum semidefinite rank of G or $\text{msr}(G)$ to be the minimum rank over all matrices in $P(G)$. We provide a characterization of graphs G for which $\text{msr}(G)=3$ and some necessary conditions for when $\text{msr}(G)$ is equal to $\text{ts}(G) - 1$, where $\text{ts}(G)$ is defined to be the number of vertices in a maximum induced tree of G . (Received July 22, 2008)