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Stefan Richter* (richter@math.utk.edu), Department of Mathematics, University of Tennessee, Knoxville, TN 37996, and **Carl Sundberg**. *Extremals for the families of commuting spherical contractions and their adjoints*. Preliminary report.

Let $d \geq 1$ and let \mathcal{F} denote the family of all commuting spherical contractions, i.e. those commuting d -tuples $T = (T_1, \dots, T_d)$ of Hilbert space operators satisfying $\sum_{j=1}^d T_j^* T_j \leq I$. Then the family of adjoint tuples, \mathcal{F}^* , consists of the d -contractions. They satisfy $\|\sum_{j=1}^d T_j x_j\|^2 \leq \sum_{j=1}^d \|x_j\|^2$ for all x_1, \dots, x_d in the Hilbert space. An operator tuple S acting on \mathcal{H} is called an extremal for a family \mathcal{G} , if and only if the only way to extend S to a tuple $T \in \mathcal{G}$ acting on $\mathcal{K} \supseteq \mathcal{H}$ is by taking direct sums. It is a theorem of Agler that every operator tuple in a family can be extended to an extremal.

We show that the extremals of the spherical contractions \mathcal{F} are of the form $S^* \oplus U$, where S is the d -shift tuple acting on a Drury-Arveson space and U is a spherical unitary tuple. The resulting extension theorem had been known and is due to Mueller-Vasilescu and to Arveson.

It appears to be unknown what the extremals for the d -contractions \mathcal{F}^* are. We characterize all extremals T of \mathcal{F}^* which satisfy that the defect operator $I - \sum_{j=1}^d T_j T_j^*$ has rank zero or one. (Received September 12, 2008)