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By means of a characterization of compact spaces in terms of open  $C^*(D)$ -filters induced by a subset  $D$  of  $C^*(X)$ , an open  $C^*(D)$ -filter process of compactification of an arbitrary topological spaces  $X$  is obtained by embedding  $X$  as a dense subspace of  $(X^*, T)$  where  $X^* = [P : P \text{ is an open } C^*(D)\text{-filter on } X]$ ,  $U^* = [P : U \text{ is in } P]$  and  $T$  is the topology induced by the base  $B = [U^* : U \text{ is a nonempty open set in } X]$  for  $X^*$ . An arbitrary Hausdorff compactification  $(Z, h)$  of a Tychonoff space  $X$  can be obtained from  $D = [f : f = *f \circ h, *f \text{ is in } C(Z)]$ , a base  $G(D)$  for  $X$  and  $X^* = [F : F \text{ is a basic } G(D)\text{-filter on } X]$  by the open  $C^*(D)$ -filter process of compactification. Finally, necessary and sufficient conditions for vector sublattices or subalgebras to be dense in  $C(Z)$ ,  $C^*(X)$  or  $C^*(Y)$  are provided as generalized Stone-Weierstrass theorems, where  $Z$ ,  $X$  and  $Y$  are a compact Hausdorff space, a Tychonoff space and an arbitrary topological space, respectively. (Received September 08, 2008)