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**Christopher J Winfield\*** (winfielc@uwosh.edu), Mathematics Dept., 800 Algoma Boulevard, Oshkosh, WI 54901. *Type Ia Supernova Luminosity Data and the LTB Model: A Well-posedness Problem*. Preliminary report.

Solutions to the Einstein equation given by the spherically symmetric Lemaître-Tolman-Bondi metric (on  $\mathbb{R}^4$ ) are studied where data is prescribed in terms of a so-called redshift parameter  $z \geq 0$ . As such solutions are characterized by functions  $E(r)$ ,  $M(r)$ , and  $R(t, r)$  satisfying

$$\left(\frac{\partial_t R}{R}\right)^2 = \frac{2E}{R^2} + \frac{2M}{R^3},$$

we study maps of the form  $\{E(r(z)), D_L(z), R(0, r(z))\} \rightarrow M(r(z))$  for observable  $D_L(z)$  [Chung, Romano: arXiv:astro-ph/0608403v1]. Here  $D_L$  is incorporated into the solution by  $D_L(z) = (1+z)^2 R(t(z), r(z))$  where  $(t(z), r(z))$  lie on certain null (photon) geodesics (i.e.  $ds^2 = 0$ ). We investigate the well-posedness of the resulting system of ordinary differential equations

$$\frac{dr}{dz} = \frac{\sqrt{1 + 2E(r(z))}}{(1+z)\partial_t \partial_r R(t(r), r(z))}$$
$$\frac{dt}{dz} = \frac{|\partial_r R(t(z), r(z))|}{(1+z)\partial_t \partial_r R(t(r), r(z))}.$$

We further discuss possible directions and how our investigation pertains to cosmological models such as dark-energy, inhomogeneous matter distribution, and the cosmological constant. (Received September 16, 2008)