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Bluffton, OH 45817. *Juggling sequences with number theory—“A tale of two kingdoms”*.

Certain infinite sequences have the property that an initial sum equals a middle sum. For example, the simple sequence  $1, 2, 3, 4, \dots$  has an initial sum of  $1 + 2 + 3 + 4 + 5 + 6$  equaling 21 which is also the value of the middle sum  $10 + 11$ . We will explore whether or how this property holds for the sequences of even and odd numbers, the Fibonacci sequence, as well as the sequence:  $1, 7, 19, \dots, (3i(i + 1) + 1), \dots$ . Surprisingly enough, the answers to these questions lead to a number-theoretic resolution for an “anthropo-mathematical” tale of the cultural clash between two kingdoms respectively valuing monistic and dualistic sequential periodic juggling. (Received September 16, 2008)