

1056-05-1731

Raluca Gera, Naval Postgraduate School, **Grady Bullington** (eroh@uwosh.edu), University of Wisconsin Oshkosh, **Linda Eroh*** (eroh@uwosh.edu), University of Wisconsin Oshkosh, 800 Algoma Blvd., Oshkosh, WI 54963, and **Steven J Winters**, University of Wisconsin Oshkosh. *On k -circuit distance in graphs.*

A delivery person must leave a central location, deliver packages at a number of addresses, and return. Naturally, he/she wishes to find the most efficient route. This motivated the definition of $(k-1)$ -stop-return distance by Gadzinski, Sanders, and Xiong, now called k -circuit distance. Given a set of k distinct vertices $\mathcal{S} = \{x_1, x_2, \dots, x_k\}$ in a simple graph G , the k -circuit-distance of set \mathcal{S} is defined to be

$$d_k(\mathcal{S}) = \min_{\theta \in \mathcal{P}(\mathcal{S})} \left(d(\theta(x_1), \theta(x_2)) + d(\theta(x_2), \theta(x_3)) + \dots + d(\theta(x_k), \theta(x_1)) \right),$$

where $\mathcal{P}(\mathcal{S})$ is the set of all permutations from \mathcal{S} onto \mathcal{S} . Thus, $d_k(x_1, \dots, x_k)$ is the length of the shortest circuit through the vertices $\{x_1, \dots, x_k\}$.

The 2-circuit distance is twice the standard distance between two vertices. We present results about the k -circuit radius, k -circuit diameter, k -circuit center and k -circuit periphery, with particular attention to $k = 3$. We also note some relationships between k -circuit distance and Steiner distance. (Received September 22, 2009)