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28804-8511. *The $L(2, 1)$ channel-assignment problem on trees.* Preliminary report.

Let $G = (V, E)$ be a simple graph. We say that a non-negative integer labeling ℓ of its vertices V is called an $L(2, 1)$ -labeling if for every pair $\{u, v\}$ of adjacent vertices $|\ell(u) - \ell(v)| \geq 2$, and for every pair $\{u, v\}$ satisfying $\rho(u, v) = 2$, $|\ell(u) - \ell(v)| \geq 1$, where ρ is the usual path metric on V . (Such labelings model the assignment of non-interfering “channels” to nearby radio transmitters.) The $L(2, 1)$ -span of a graph G , $\lambda(G)$, is defined to be the minimum value, over all $L(2, 1)$ -labelings of G , of $\max_{v \in V} \ell(v)$.

In 1992 J.R. Griggs and R.K. Yeh proved that for a tree T with maximal vertex degree Δ , $\lambda(T) \in \{\Delta + 1, \Delta + 2\}$, but conjectured that for an arbitrary tree determining which of these values obtains would prove to be NP-hard.

We describe a deterministic algorithm for computing $\lambda(T)$ in the case $\Delta = 3$ and indicate how this algorithm can be generalized to arbitrary maximal degree Δ . The algorithm has exponential time complexity, and its construction shows why no more efficient deterministic algorithm can be found. (Received July 21, 2009)