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Pósa proved that if  $G$  is an  $n$ -vertex graph in which any two nonadjacent vertices have degree sum at least  $n + k$ , then  $G$  has a spanning cycle containing any specified family of disjoint paths with a total of  $k$  edges. We consider the analogous problem for a bipartite graph  $G$  with  $n$  vertices and parts of equal size. Let  $F$  be a subgraph of  $G$  whose components are nontrivial paths. Let  $k$  be the number of edges in  $F$ , and let  $t_1$  and  $t_2$  be the numbers of components of  $F$  having odd and even length, respectively. For  $n \geq 9k + 4$ , there is a spanning cycle in  $G$  containing  $F$  if any two nonadjacent vertices in opposite partite sets have degree-sum at least  $n/2 + \tau(F)$ , where  $\tau(F) = \lceil k/2 \rceil + \epsilon$  (here  $\epsilon = 1$  if  $t_1 = 0$  or if  $(t_1, t_2) \in \{(1, 0), (2, 0)\}$ , and  $\epsilon = 0$  otherwise). The threshold on the degree-sum is sharp. (Received September 18, 2009)