

1056-35-1615

Jaffar Ali* (jahameed@fgcu.edu), #450, Library, Florida Gulf Coast University, 10501 FGCU Blvd. S., Fort Myers, FL 33965, and **Ratnasingham Shivaji** (shivaji@ra.msstate.edu), Department of Mathematics, Mississippi State University, Mississippi State, MS 39759. *Multiple positive solutions for a class of p - q -Laplacian systems with multiple parameters and combined nonlinear effects.*

Consider the system

$$\begin{cases} -\Delta_p u &= \lambda_1 f(v) + \mu_1 h(u), \text{ in } \Omega \\ -\Delta_q v &= \lambda_2 g(u) + \mu_2 \gamma(v), \text{ in } \Omega \\ u = 0 = v, &\text{ on } \partial\Omega \end{cases}$$

where $\Delta_s z = \operatorname{div}(|\nabla z|^{s-2} \nabla z)$; $s > 1$, $\lambda_1 > 0$, $\lambda_2 > 0$, $\mu_1 \geq 0$ and $\mu_2 \geq 0$ are parameters and Ω is a bounded domain in R^n with smooth boundary $\partial\Omega$. For some classes of non-negative monotone functions f, g, h and γ which satisfy

$$\lim_{x \rightarrow \infty} \frac{f(M[g(x)]^{1/q-1})}{x^{p-1}} = 0, \quad \forall M > 0,$$

$\lim_{x \rightarrow \infty} \frac{h(x)}{x^{p-1}} = 0$ and $\lim_{x \rightarrow \infty} \frac{\gamma(x)}{x^{q-1}} = 0$, we discuss the existence of multiplicity of positive solutions for certain range of parameters $\lambda_1, \mu_1, \lambda_2$ and μ_2 . We use the method of sub- and super-solutions to establish our results.

(Received September 22, 2009)