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We consider the problem  $-\Delta u = \lambda(u - \varphi)_+^{p-1}$ ,  $x \in \Omega$ ,  $u|_{\partial\Omega} = 0$ , where  $\Omega$  is a bounded domain in  $\mathbb{R}^N$ ,  $\varphi$  is a positive harmonic function in  $\bar{\Omega}$ .

This problem is related to steady vortex pairs in an ideal fluid. Under the following condition:  $\varphi$  has  $k$  ( $k \geq 1$ ) strictly local minimum points  $\bar{z}_1, \dots, \bar{z}_k \in \partial\Omega$ , we are able to prove the existence of a solution pair  $(u_\lambda, A_\lambda)$  satisfying that the “vortex core” (where  $u_\lambda > \varphi$ )  $A_\lambda$  has exactly  $k$  components  $A_{\lambda,j}$ ,  $j = 1, \dots, k$  which shrink to the points  $\bar{z}_1, \dots, \bar{z}_k$  respectively as  $\lambda \rightarrow +\infty$ . Moreover,  $A_{\lambda,j}$  is approximately a ball with very precise estimates of  $z_j - \bar{z}_j$  and  $diam(A_{\lambda,j})$ . (Received September 22, 2009)