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Given $\Omega, \Omega^* \subset S^{n-1}$; two positive functions $f \in L^1(\Omega), g \in L^1(\Omega^*)$; and two homogeneous media I and II with indices of refraction n_1 and n_2 respectively, suppose from a light source at the origin O inside medium I, a light ray emanates with intensity $f(x), x \in \Omega$ and hits an interface \mathcal{R} between media I and media II. Then the ray of light bends in a direction m according to Snell's law, and it also loses its intensity by a factor according to Fresnel's formulas. Set $x = \mathcal{T}_{\mathcal{R}}(m)$. Finding the weak solution of the general refractor problem for a light beam with illumination intensity f and prescribed illumination intensity g involves finding a radial graph

$$\mathcal{R} = \{x\rho(x)|x \in \Omega\}$$

such that for every Borel set $\omega \subset \Omega^*$

$$\int_{\mathcal{T}_{\mathcal{R}}(\omega)} f(x)t_{\mathcal{R}}(x)dx = \int_{\omega} g(m)dm$$

where $t_{\mathcal{R}}(x)$ is the fraction of intensity lost as given by Fresnel's formulas. In this work we will use ellipsoidal approximation to solve the problem. Moreover we notice that the solution satisfies a fully nonlinear partial differential equation of Monge - Ampère type. This is joint work with Prof. C. E. Gutierrez. (Received September 18, 2009)