

1056-42-819

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The problem of constructing Parseval frames for  $L^2(\mathbb{R}^n)$  of the form

$$\{\sqrt{c(x, \nu)} e^{2\pi i t \nu} g(t - x)\}_{(x, \nu) \in \Lambda},$$

where  $g \in L^2(\mathbb{R}^n)$  with  $\|g\|_2 = 1$ ,  $\Lambda$  is a discrete subset of the time-frequency space  $\mathbb{R}^{2n}$  and  $c(x, \nu) > 0$  for  $(x, \nu) \in \Lambda$ , leads naturally to the question of finding discrete positive measures  $\mu$  on  $\mathbb{R}^{2n}$  satisfying the identity

$$\int_{\mathbb{R}^{2n}} |V_g f(x, \nu)|^2 d\mu(x, \nu) = \|f\|_2^2, \quad f \in L^2(\mathbb{R}^n),$$

where  $V_g$  denotes the short-time Fourier transform with window  $g$ . When  $g$  is a function in the Schwartz class  $\mathcal{S}(\mathbb{R}^n)$ , a recent result of the author shows that the isometric embedding above is equivalent to the identity  $\mathcal{F}^S(\mu) V_g g = \delta_{(0,0)}$ , where  $\mathcal{F}^S(\mu)$  denote the symplectic Fourier transform of  $\mu$ . The focus of this talk will be to provide an alternative to this formula when  $g$  is an arbitrary window in  $L^2(\mathbb{R}^n)$  (in which case the distributional product in the previous formula no longer makes sense) and to discuss some of its consequences. (Received September 17, 2009)