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For M a manifold, let $\rho_t(x, y)$ denote a non-negative kernel on $M \times M$ satisfying the semi-group property in time t . Peter Jones has proposed the following natural measure of discrepancy between two points x and y in M : for a fixed parameter ω with $0 < \omega < 1$,

$$\tau(x, y) = \operatorname{argmin}_t \left\{ \int_M \min(\rho_t(u, x), \rho_t(u, y)) du \geq \omega \right\},$$

i.e. $\tau(x, y)$ is the first time that the two “bump” functions centered at x and y , respectively, significantly overlap. In the case of heat flow on \mathbb{R}^n , $\tau(x, y)$ is a scaled square of the usual Euclidean distance; in particular, $\tau(\cdot, \cdot)$ does not satisfy the triangle inequality.

We propose a general construction which modifies $\tau(x, y)$ so that the result does satisfy the triangle inequality (with possible minor exceptions), and hence is (almost) a metric. In the case of heat flow on \mathbb{R}^n , our method recovers scaled Euclidean distance. (Received September 19, 2009)