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*Four-dimensional metrics conformal to Kahler.*

I shall discuss my recent work with Paul Tod and give some necessary and sufficient conditions on a Riemannian metric  $(M, g)$  in four dimensions for it to be locally conformal to Kähler. If the conformal curvature is non anti-self-dual, the self-dual Weyl spinor must be of algebraic type  $D$  and satisfy a simple first order conformally invariant condition which is sufficient and necessary for the existence of a Kähler metric in the conformal class. In the anti-self-dual case we establish a one to one correspondence between Kähler metrics in the conformal class and non-zero parallel sections of a certain connection on a natural rank ten vector bundle over  $M$ . We use this characterisation to provide examples of ASD metrics which are not conformal to Kähler. We establish a link between the ‘conformal to Kähler condition’ in dimension four and the metrisability of projective structures in dimension two. A projective structure on a surface  $U$  is metrisable if and only if the induced  $(2, 2)$  conformal structure on  $M = TU$  admits a Kähler metric or a para-Kähler metric. (Received September 12, 2009)