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PO Box 400137, Charlottesville, VA 22904. *Stabilization of Homotopy Limits.*

This talk will outline the major results of my thesis work, which describes a natural filtration, inspired by Goodwillie's Calculus of Functors, of the stable homotopy type of the space  $\mathrm{holim}_{\mathcal{C}} F$  for a given functor  $F : \mathcal{C} \rightarrow \mathcal{T}op$ , where  $\mathcal{C}$  is some small indexing category. More concretely, we construct a sequence of categories  $\mathcal{C} = \mathcal{C}_1 \subseteq \mathcal{C}_2 \subseteq \mathcal{C}_3 \cdots$  derived from  $\mathcal{C}$  such that, under favorable conditions, we have an equivalence

$$\Sigma^\infty \mathrm{holim}_{\mathcal{C}} F \simeq \mathrm{holim} (\cdots \rightarrow \mathrm{holim}_{\mathcal{C}_2} \Sigma^\infty F \rightarrow \mathrm{holim}_{\mathcal{C}_1} \Sigma^\infty F)$$

When  $F$  is constant, we recover the results of G. Arone on the derivatives of the functor  $\Sigma^\infty \mathrm{Map}(K, X)$ , whereas for  $\mathcal{C}$  discrete we recover the classical Snaith splitting of a product. The spectral sequence obtained from this filtration can be considered as an alternative to the Bousfield-Kan spectral sequence of a cosimplicial space. (Received September 22, 2009)